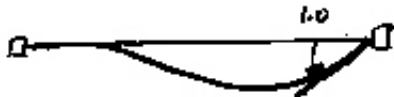


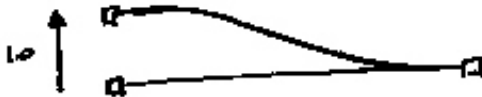
$$f_1(x) = -\frac{1}{L^2} [L^2 x - 2Lx^2 + x^3]$$

$$\frac{df_1}{dx^2} = -\frac{1}{L^2} [-4L + 6x]$$



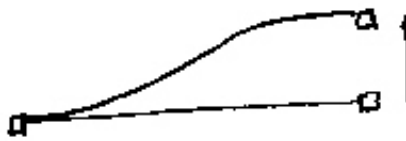
$$f_2(x) = -\frac{1}{L^2} (-Lx^2 + x^3)$$

$$\frac{df_2}{dx^2} = -\frac{1}{L^2} [-2L + 6x]$$



$$f_3(x) = -\frac{1}{L^3} (L^3 - 3Lx^2 + 2x^3)$$

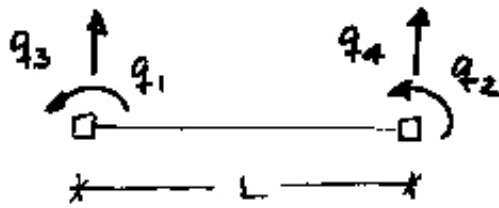
$$\frac{df_3}{dx^2} = -\frac{1}{L^3} [-6L + 12x]$$



$$f_4(x) = -\frac{1}{L^3} (3Lx^2 - 2x^3)$$

$$\frac{df_4}{dx^2} = -\frac{1}{L^3} [6L - 12x]$$

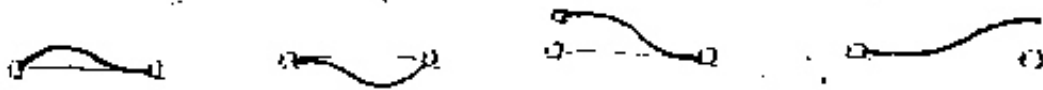
ELEMENTO DE VIGA



MATRIZ DE RIGIDEZ ELEMENTAR

$$K^{(e)} = \int_0^L \begin{bmatrix} \frac{1}{L^2}(-4L+6x) & \frac{1}{L^2}(-2L+6x) & \frac{1}{L^3}(-6L+12x) & \frac{1}{L^3}(6L-12x) \end{bmatrix} EI \begin{bmatrix} \frac{1}{L^2}(-4L+6x) \\ \frac{1}{L^2}(-2L+6x) \\ \frac{1}{L^3}(-6L+12x) \\ \frac{1}{L^3}(6L-12x) \end{bmatrix} dx$$

$$K^{(e)} = \begin{bmatrix} 4EI/L & 2EI/L & 6EI/L^2 & -6EI/L^2 \\ 2EI/L & 4EI/L & 6EI/L^2 & -6EI/L^2 \\ 6EI/L^2 & 6EI/L^2 & 12EI/L^3 & -12EI/L^3 \\ -6EI/L^2 & -6EI/L^2 & -12EI/L^3 & 12EI/L^3 \end{bmatrix}$$

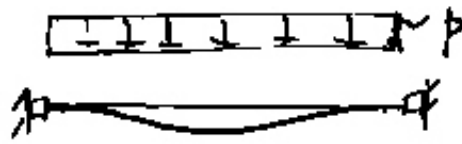


VECTOR DAS FORÇAS NODAIS EQUIVALENTES

$$F^{(e)} = \int_0^L \begin{bmatrix} -\frac{1}{L^2}(L^2x - 2Lx^2 + x^3) \\ -\frac{1}{L^2}(-Lx^2 + x^3) \\ -\frac{1}{L^3}(L^3 - 3Lx^2 + 2x^3) \\ -\frac{1}{L^3}(3Lx^2 - 2x^3) \end{bmatrix} [p(x)] dx$$



□



$$F^{(e)} = \int_0^L \begin{bmatrix} f_1(x) \times p(x) \\ f_2(x) \times p(x) \\ f_3(x) \times p(x) \\ f_4(x) \times p(x) \end{bmatrix} dx$$

$$F^{(e)} = \begin{bmatrix} -pL^2/12 \\ pL^2/12 \\ -pL/2 \\ -pL/2 \end{bmatrix}$$